

TECHNOLOGY CORNER for Section 2.2, Page 116

5. From Z-Scores to Area, and Vice Versa

Finding areas: The `NORMALD_CDF()` command on the HP Prime can be used to find lower-tail areas under a Normal curve. The syntax is `NORMALD_CDF(mean, standard deviation, value)` and it returns the area to the left of *value* under a Normal cumulative density function with the given *mean* and *standard deviation*.

1. What proportion of observations from the standard Normal distribution are greater than -1.78 ? Recall that the standard Normal distribution has mean 0 and standard deviation 1. Since this calculation involves the area to the right of $z = -1.78$, we use `1-NORMAL_CDF(0,1,-1.78)`.

- Press to go to Home view
- Type 1-, then press , tap **Math** if not already selected, tap **Probability**, tap **Cumulative**, and tap **Normal** to select the Normal cumulative density function `NORMALD_CDF(μ, σ, x)`
- Press ; then press to complete the formula

The mean and standard deviation are optional for the standard Normal curve, so `1-NORMAL_CDF(-1.78)` returns the same result.

- Also, using -1.78 as the lower bound and $1E99$ as the upper bound returns the same result without subtracting the normal calculation from 1

| | |
|--|----------------|
| <code>1-NORMALD_CDF(0,1,-1.78)</code> | 0.962462019652 |
| <code>1-NORMALD_CDF(-1.78)</code> | 0.962462019652 |
| <code>NORMALD_CDF(0,1,-1.78,1E99)</code> | 0.962462019652 |




2. What proportion of observations from the standard Normal distribution is between -1.25 and 0.81 ? In this case, we subtract two areas to find the area between the two values.
 - Also, using -1.25 as the lower bound and $.81$ as the upper bound returns the same area

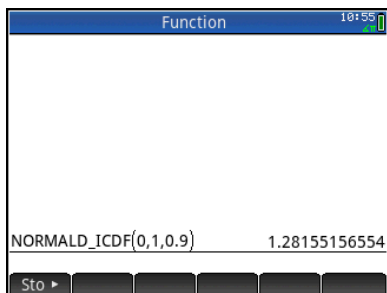
The screen shot below confirms the result of 0.6854 using Table A.

| | |
|---|----------------|
| <code>NORMALD_CDF(0.81)-NORMALD_CDF(-1.25)</code> | 0.685380138461 |
| <code>NORMALD_CDF(0,1,-1.25,0.81)</code> | 0.685380138461 |

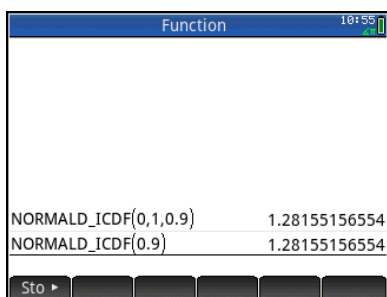
Working backward: The HP Prime `NORMALD_ICDF()` function calculates the z-value corresponding to a given percentile in a Normal distribution. For this command, the syntax is `NORMAL_ICDF (mean, standard deviation, area to the left)`.

3. What is the 90th percentile of the standard Normal distribution?

- Press , if not already selected tap , tap **Probability**, tap **Inverse**, and tap **Normal** to select the Normal inverse cumulative density function `NORMALD_ICDF(μ , σ , x)`
- Complete the formula `NORMALD_ICDF(0, 1, 0.9)` and press  .



- For the standard Normal distribution, you can omit the mean and standard deviation and just enter `NORMALD_ICDF(0.9)` as shown below.



The results match what we got using Table A.